Chapter 2: Surface Area and Volume 2.1 Surface Area of Prisms and Cylinders

Outcomes: Solve problems, using SI and imperial units, that involve the surface area of 3-D objects, including right prisms and cylinders.

Review:

1) Find the area of a triangle, where the base is 4cm and the height is 10 cm

2) Find the area of a rectangle where the length is 12 m and the width is 7 m

Definitions:

Surface Area: the sum of the areas of each face of the object.

ALWAYS MEASURED IN SQUARE UNITS

<u>Prisms:</u> three-dimensional object which has two bases or ends that have the same size and shape and are parallel to each other.

Cylinder: Three-dimensional object with two parallel and congruent circular bases.

Example 1:

Identify what three-dimensional shape is and the surface area of the shape below.



Example 2:

Identify what three-dimensional shape is and the surface area of the shape below.



Example 3:

Identify what three-dimensional shape is and the surface area of the shape below.



Example 4: Find the width if the SA = 500cm²





Textbook Questions: Pg. 74 # 1ab, 3ab, 4, 6, 9, 11, 17

2.2 Surface Area of Pyramids and Cones

Outcomes: Solve problems, using SI and imperial units, that involve the surface area of 3-D objects, including right pyramids and cones.

Definitions:

<u>Pyramid</u>: A three-dimensional object with one base and the same number of triangular faces as there are sides on the base.

For example: Square-based Pyramid; Rectangular Pyramid; Triangular Pyramid

<u>Cone:</u> Three-dimensional object with a circular base and a curved lateral side that extends from the base to the vertex.

<u>Slant Height:</u> the shortest lateral distance from the edge of the base of a pyramid to its highest point.

<u>Lateral Area</u>: the surface that joins the two bases of a three-dimensional object or that joins the base to the highest point

Review:

Find the area of a circle with:

- a) Diameter of 6ft
- b) Radius of 2cm

Example 1:

Calculate the surface area of the tetrahedron pyramid.



Example 2:

A right rectangular pyramid has base dimensions 8ft by 10ft, and a height of 16ft. Calculate the surface area of the pyramid to the nearest square foot.



Surface Area of a Cone:



Example 3:

A right cone has a base radius of 2ft and a height of 7ft. Calculate the surface area of the cone to the nearest foot.



Example 4:

The lateral area of a cone is 220 cm^2 . The diameter of the cone is 10 cm. Determine the height of the cone, to the nearest tenth of a cm.



Textbook Questions: Pg. 74. #1cd, 2, 7, 12, 14, 16

2.3 Surface Area Spheres

Outcomes: Solve problems, using SI and imperial units, that involve the surface area of 3-D objects, including spheres

Definitions:

Sphere: a round, ball-shaped object

A set of points in space that are a given distance (radius) from a fixed point (centre)

Surface Area of a Sphere:

$$SA = 4\pi r^2$$

Example 1:

The diameter of a baseball is approximately 3 in. Determine the surface area of a baseball to the nearest square inch.

Example 2:

The surface area of a lacrosse ball is approximately 20 square inches. What is the diameter of the lacrosse ball to the nearest tenth of an inch.

Textbook Questions: Pg. 74 #1e, 3c, 5, 13, 15

2.4 Volume of Prisms, Cylinders and Spheres

Outcomes: Solve problems, using SI and imperial units, that involve the volume of 3-D objects, including right prisms, right cylinders, and spheres.

To calculate the volume of prisms and cylinders, simply calculate the area of the base then multiply by the height.

Example 1:

1. Calculate the volume of each shape:







C)



To calculate the volume of a sphere, use the formula $V = \frac{4}{3}\pi r^3$

2. Calculate the volume of the sphere that has a radius of 4.5 inches.

3. A hemisphere has a radius of 8 cm.

a) What is the surface area of the hemisphere to the nearest tenth of a square cm?



b) What is the volume of the hemisphere to the nearest tenth of a cubic cm?

Textbook Questions: Pg. 86 #1(bce), 3, 5(ac), 6-8, 13, 14

2.5 Volume of Pyramids and Cones

Outcomes: Solve problems, using SI and imperial units, that involve the volume of 3-D objects, including right pyramids and cones.

To calculate the volume of pyramids, use the following formula:

$$V = \frac{1}{3}lwh$$

To calculate the volume of cones, use the following formula:

$$V = \frac{1}{3}\pi r^2 h$$



5.4 m

C)

1. Calculate the volume of each shape:

2. A cone has a height of 4 yd and a volume of 205 cubic yards. Determine the radius of the base of the cone to the nearest whole number.

Textbook Questions: Pg. 86 # 1(ab), 2(ab), 9 - 11, 12, 18